

67. You are given the following information about a book of business comprised of 100 insureds:

- (i) $X_i = \sum_{j=1}^{N_i} Y_{ij}$ is a random variable representing the annual loss of the i^{th} insured.
- (ii) N_1, N_2, \dots, N_{100} are independent random variables distributed according to a negative binomial distribution with parameters r (unknown) and $\beta = 0.2$.
- (iii) Unknown parameter r has an exponential distribution with mean 2.
- (iv) $Y_{i1}, Y_{i2}, \dots, Y_{iN_i}$ are independent random variables distributed according to a Pareto distribution with $\alpha = 3.0$ and $\theta = 1000$.

Determine the Bühlmann credibility factor, Z , for the book of business.

- (A) 0.000
- (B) 0.045
- (C) 0.500
- (D) 0.826
- (E) 0.905