

Question #162**Key: B**

$E[x-d|x>d]$ is the expected payment per payment with an ordinary deductible of d

It can be evaluated (for Pareto) as

$$\begin{aligned} \frac{E(x) - E(x \wedge d)}{1 - F(d)} &= \frac{\frac{\theta}{\alpha - 1} - \frac{\theta}{\alpha - 1} \left[1 - \left(\frac{\theta}{d + \theta} \right)^{\alpha - 1} \right]}{1 - \left[1 - \left(\frac{\theta}{d + \theta} \right)^{\alpha} \right]} \\ &= \frac{\frac{\theta}{\alpha - 1} \left(\frac{\theta}{d + \theta} \right)^{\alpha - 1}}{\left(\frac{\theta}{d + \theta} \right)^{\alpha}} \\ &= \frac{d + \theta}{\alpha - 1} \\ &= d + \theta \text{ in this problem, since } \alpha = 2 \end{aligned}$$

$$E[x - 100 | x > 100] = \frac{5}{3} E[x - 50 | x > 50]$$

$$100 + \theta = \frac{5}{3}(50 + \theta)$$

$$300 + 3\theta = 250 + 5\theta$$

$$= \theta = 25$$

$$E[x - 150 | x > 150] = 150 + \theta$$

$$= 150 + 25$$

$$= 175$$