

3. An insurance company sells single premium deferred annuity contracts with return linked to a stock index, the time- t value of one unit of which is denoted by $S(t)$. The contracts offer a minimum guarantee return rate of $g\%$. At time 0, a single premium of amount π is paid by the policyholder, and $\pi \times y\%$ is deducted by the insurance company. Thus, at the contract maturity date, T , the insurance company will pay the policyholder

$$\pi \times (1 - y\%) \times \text{Max}[S(T)/S(0), (1 + g\%)^T].$$

You are given the following information:

- (i) The contract will mature in one year.
- (ii) The minimum guarantee rate of return, $g\%$, is 3%.
- (iii) Dividends are incorporated in the stock index. That is, the stock index is constructed with all stock dividends reinvested.
- (iv) $S(0) = 100$.
- (v) The price of a one-year European put option, with strike price of \$103, on the stock index is \$15.21.

Determine $y\%$, so that the insurance company does not make or lose money on this contract.