

**53.** The mortality of  $(x)$  and  $(y)$  follows a common shock model with states:

State 0 – both alive

State 1 – only  $(x)$  alive

State 2 – only  $(y)$  alive

State 3 – both dead

You are given:

(i)  $\mu_{x+t} = \mu_{x+t;y+t}^{02} + \mu_{x+t;y+t}^{03} = \mu_{x+t;y+t}^{13} = g$ , a constant,  $0 \leq t \leq 5$

(ii)  $\mu_{y+t} = \mu_{x+t;y+t}^{01} + \mu_{x+t;y+t}^{03} = \mu_{x+t;y+t}^{23} = h$ , a constant,  $0 \leq t \leq 5$

(iii)  $p_{x+t} = 0.96$ ,  $0 \leq t \leq 4$

(iv)  $p_{y+t} = 0.97$ ,  $0 \leq t \leq 4$

(v)  $\mu_{x+t;y+t}^{03} = 0.01$ ,  $0 \leq t \leq 5$

Calculate the probability that  $(x)$  and  $(y)$  both survive 5 years.

(A) 0.65

(B) 0.67

(C) 0.70

(D) 0.72

(E) 0.74