

Question #98

Answer: E

For the general survival function $S_0(t) = 1 - \frac{t}{\omega}$, $0 \leq t \leq \omega$,

$$\begin{aligned}\dot{e}_{30} &= \int_0^{\omega-30} \left(1 - \frac{t}{\omega-30}\right) dt \\ &= \left[t - \frac{t^2}{2(\omega-30)} \right]_0^{\omega-30} \\ &= \frac{\omega-30}{2}\end{aligned}$$

Prior to medical breakthrough $\omega = 100 \Rightarrow \dot{e}_{30} = \frac{100-30}{2} = 35$

After medical breakthrough $\dot{e}'_{30} = \dot{e}_{30} + 4 = 39$

$$\text{so } \dot{e}'_{30} = 39 = \frac{\omega' - 30}{2} \Rightarrow \omega' = 108$$