

Question #167

Answer: A

$${}_5p_{50}^{(\tau)} = e^{-(0.05)(5)} = e^{-0.25} = 0.7788$$

$$\begin{aligned} {}_5q_{55}^{(1)} &= \int_0^5 \mu_{55+t}^{(1)} \times e^{-(0.03+0.02)t} dt = -(0.02 / 0.05) e^{-0.05t} \Big|_0^5 \\ &= 0.4(1 - e^{-0.25}) \\ &= 0.0885 \end{aligned}$$

$$\begin{aligned} \text{Probability of retiring before } 60 &= {}_5p_{50}^{(\tau)} \times {}_5q_{55}^{(1)} \\ &= 0.7788 \times 0.0885 \\ &= 0.0689 \end{aligned}$$