

Question #196

Answer: E

If (40) dies before 70, he receives one payment of 10, and $Y = 10$. The probability of this is $(70 - 40)/(110 - 40) = 3/7$

If (40) reaches 70 but dies before 100, he receives 2 payments.

$$Y = 10 + 20v^{30} = 16.16637$$

The probability of this is also $3/7$.

If (40) survives to 100, he receives 3 payments.

$$Y = 10 + 20v^{30} + 30v^{60} = 19.01819$$

The probability of this is $1 - 3/7 - 3/7 = 1/7$

$$E(Y) = (3/7) \times 10 + (3/7) \times 16.16637 + (1/7) \times 19.01819 = 13.93104$$

$$E(Y^2) = (3/7) \times 10^2 + (3/7) \times 16.16637^2 + (1/7) \times 19.01819^2 = 206.53515$$

$$\text{Var}(Y) = E(Y^2) - [E(Y)]^2 = 12.46$$

Since everyone receives the first payment of 10, you could have ignored it in the calculation.