

Question #219

Answer: E

$${}_{0.25|1.5}q_x = {}_{0.25}p_x - {}_{1.75}p_x$$

Let μ be the force of mortality in year 1, so 3μ is the force of mortality in year 2.

Probability of surviving 2 years is 10%

$$\begin{cases} 0.10 = p_x p_{x+1} = e^{-\mu} e^{-3\mu} = e^{-4\mu} \\ \mu = \frac{\ln(0.1)}{4} = 0.5756 \end{cases}$$

$${}_{0.25}p_x = e^{-\frac{1}{4}(0.5756)} = 0.8660$$

$${}_{1.75}p_x = p_x \times {}_{0.75}p_{x+1} = e^{-\mu} e^{-\frac{3}{4}(3\mu)} = e^{-\frac{13}{4}(0.5756)} = 0.1540$$

$${}_{1.5}q_{x+0.25} = \frac{{}_{0.25|1.5}q_x}{{}_{0.25}p_x} = \frac{{}_{0.25}p_x - {}_{1.75}p_x}{{}_{0.25}p_x} = \frac{0.866 - 0.154}{0.866} = 0.82$$