

Question #247

Answer: C

EPV (expected present value) of benefits = 3499 (given)

$$\begin{aligned}\text{EPV of premiums} &= G + (0.9)(G)v \\ &= G + \frac{0.9G}{1.05} = 1.8571G\end{aligned}$$

EPV of expenses, except settlement expenses,

$$\begin{aligned}&= [25 + (4.5)(10) + 0.2G] + (0.9)[10 + (1.5)(10) + 0.1G]v + (0.9)(0.85)[10 + (1.5)(10)]v^2 \\ &= 70 + 0.2G + \frac{0.9(25 + 0.1G)}{1.05} + \frac{0.765(25)}{1.05^2} \\ &= 108.78 + 0.2857G\end{aligned}$$

Settlement expenses are $20 + (1)(10) = 30$, payable at the same time the death benefit is paid.

$$\begin{aligned}\text{So EPV of settlement expenses} &= \left(\frac{30}{10,000} \right) \text{EPV of benefits} \\ &= (0.003)(3499) \\ &= 10.50\end{aligned}$$

Equivalence principle:

$$\begin{aligned}1.8571G &= 3499 + 108.78 + 0.2857G + 10.50 \\ G &= \frac{3618.28}{1.8571 - 0.2857} = 2302.59\end{aligned}$$