A company offers earthquake insurance. Annual premiums are modeled by an exponential random variable with mean 2. Annual claims are modeled by an exponential random variable with mean 1. Premiums and claims are independent. Let $X$ denote the ratio of claims to premiums.

What is the density function of $X$?

(A) $\frac{1}{2x+1}$

(B) $\frac{2}{(2x+1)^2}$

(C) $e^{-x}$

(D) $2e^{-2x}$

(E) $xe^{-x}$

110. Let $X$ and $Y$ be continuous random variables with joint density function

$$f(x, y) = \begin{cases} 24xy & \text{for } 0 < x < 1 \text{ and } 0 < y < 1-x \\ 0 & \text{otherwise.} \end{cases}$$