

Problem 31

X : number of employees reaching high performance level

$X \sim \text{Binomial}(n=20, p=.02)$

Want $p(X > x) \leq .01$

Equivalently: $p(X \leq x) \geq .99$

$$\hookrightarrow p(X=0) + p(X=1) + \dots + p(X=x)$$

$$p(X=0) = \binom{20}{0} (.02)^0 (.98)^{20} = .668$$

$$p(X=1) = \binom{20}{1} (.02)^1 (.98)^{19} = .272$$

$$p(X=2) = \binom{20}{2} (.02)^2 (.98)^{18} = .053$$

<u>X</u>	<u>$p(X=x)$</u>	<u>$p(X \leq x)$</u>	
0	.668	.668	
1	.272	.94	
2	.053	.993	so $x=2$

$$2 \cdot C = 120,000$$

$$C = 60,000$$

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