

50. X : # of snowstorms

Y : Payout

$$Y = \begin{cases} 0 & X \leq 1 \\ 10,000X - 10,000 & X > 1 \end{cases} \quad E(Y) = ?$$

$$E(Y) \neq E(10,000X - 10,000)$$

$$E(10,000X - 10,000) =$$

$$-10,000 \cdot P(X=0) + 0 \cdot P(X=1) + 10,000 \cdot P(X=2) + 20,000 \cdot P(X=3) + \dots$$

We want:

$$E(Y) = 10,000 \cdot P(X=2) + 20,000 \cdot P(X=3) + 30,000 \cdot P(X=4) + \dots$$

→ notice the first term in $E(10,000X - 10,000)$ is different, so we can just take this out.

$$\rightarrow E(10,000X - 10,000) - (-10,000 \cdot P(X=0))$$

$$= 10,000E(X) - 10,000 + 10,000 \cdot P(X=0)$$

$$= 10,000(1.5) - 10,000 + 10,000e^{-1.5}$$

$$= 7231$$

(C)

$$\begin{aligned} X &\sim \text{Poisson}(\lambda=1.5) \\ P(X=k) &= \frac{\lambda^k e^{-\lambda}}{k!} \\ P(X=0) &= \frac{1.5^0 e^{-1.5}}{0!} \\ &= e^{-1.5} \\ E(X) &= 1.5 \end{aligned}$$