

59. Solution: B

The distribution function of X is given by

$$F(x) = \int_{200}^x \frac{2.5(200)^{2.5}}{t^{3.5}} dt = \left. \frac{-(200)^{2.5}}{t^{2.5}} \right|_{200}^x = 1 - \frac{(200)^{2.5}}{x^{2.5}}, \quad x > 200$$

Therefore, the p^{th} percentile x_p of X is given by

$$\frac{p}{100} = F(x_p) = 1 - \frac{(200)^{2.5}}{x_p^{2.5}}$$

$$1 - 0.01p = \frac{(200)^{2.5}}{x_p^{2.5}}$$

$$(1 - 0.01p)^{2/5} = \frac{200}{x_p}$$

$$x_p = \frac{200}{(1 - 0.01p)^{2/5}}$$

It follows that $x_{70} - x_{30} = \frac{200}{(0.30)^{2/5}} - \frac{200}{(0.70)^{2/5}} = 93.06$

60. Solution: E

Let X and Y denote the annual cost of maintaining and repairing a car before and after the 20% tax, respectively. Then $Y = 1.2X$ and $\text{Var}[Y] = \text{Var}[1.2X] = (1.2)^2 \text{Var}[X] = (1.2)^2(260) = 374$.

61. Solution: A

The first quartile, Q1, is found by $\frac{3}{4} = \int_{Q1}^{\infty} f(x) dx$. That is, $\frac{3}{4} = (200/Q1)^{2.5}$ or $Q1 = 200 (4/3)^{0.4} = 224.4$. Similarly, the third quartile, Q3, is given by $Q3 = 200 (4)^{0.4} = 348.2$. The interquartile range is the difference $Q3 - Q1$.