

63. Solution: C

$$\text{Note } Y = \begin{cases} X & \text{if } 0 \leq X \leq 4 \\ 4 & \text{if } 4 < X \leq 5 \end{cases}$$

Therefore,

$$\begin{aligned} E[Y] &= \int_0^4 \frac{1}{5} x dx + \int_4^5 \frac{4}{5} dx = \frac{1}{10} x^2 \Big|_0^4 + \frac{4}{5} x \Big|_4^5 \\ &= \frac{16}{10} + \frac{20}{5} - \frac{16}{5} = \frac{8}{5} + \frac{4}{5} = \frac{12}{5} \end{aligned}$$

$$\begin{aligned} E[Y^2] &= \int_0^4 \frac{1}{5} x^2 dx + \int_4^5 \frac{16}{5} dx = \frac{1}{15} x^3 \Big|_0^4 + \frac{16}{5} x \Big|_4^5 \\ &= \frac{64}{15} + \frac{80}{5} - \frac{64}{5} = \frac{64}{15} + \frac{16}{5} = \frac{64}{15} + \frac{48}{15} = \frac{112}{15} \end{aligned}$$

$$\text{Var}[Y] = E[Y^2] - (E[Y])^2 = \frac{112}{15} - \left(\frac{12}{5}\right)^2 = 1.71$$