

67.

Solution: B

The amount of money the insurance company will have to pay is defined by the random variable

$$Y = \begin{cases} 1000x & \text{if } x < 2 \\ 2000 & \text{if } x \geq 2 \end{cases}$$

where x is a Poisson random variable with mean 0.6 . The probability function for X is

$$p(x) = \frac{e^{-0.6} (0.6)^k}{k!} \quad k = 0, 1, 2, 3 \dots \text{ and}$$

$$\begin{aligned} E[Y] &= 0 + 1000(0.6)e^{-0.6} + 2000e^{-0.6} \sum_{k=2}^{\infty} \frac{0.6^k}{k!} \\ &= 1000(0.6)e^{-0.6} + 2000 \left(e^{-0.6} \sum_{k=0}^{\infty} \frac{0.6^k}{k!} - e^{-0.6} - (0.6)e^{-0.6} \right) \\ &= 2000e^{-0.6} \sum_{k=0}^{\infty} \frac{(0.6)^k}{k!} - 2000e^{-0.6} - 1000(0.6)e^{-0.6} = 2000 - 2000e^{-0.6} - 600e^{-0.6} \end{aligned}$$

$$= 573$$

$$\begin{aligned} E[Y^2] &= (1000)^2 (0.6)e^{-0.6} + (2000)^2 e^{-0.6} \sum_{k=2}^{\infty} \frac{0.6^k}{k!} \\ &= (2000)^2 e^{-0.6} \sum_{k=0}^{\infty} \frac{0.6^k}{k!} - (2000)^2 e^{-0.6} - \left[(2000)^2 - (1000)^2 \right] (0.6)e^{-0.6} \\ &= (2000)^2 - (2000)^2 e^{-0.6} - \left[(2000)^2 - (1000)^2 \right] (0.6)e^{-0.6} \\ &= 816,893 \end{aligned}$$

$$\text{Var}[Y] = E[Y^2] - \{E[Y]\}^2 = 816,893 - (573)^2 = 488,564$$

$$\sqrt{\text{Var}[Y]} = 699$$