

70. Solution: E

Let  $X$  denote actual losses incurred. We are given that  $X$  follows an exponential distribution with mean 300, and we are asked to find the 95<sup>th</sup> percentile of all claims that exceed 100. Consequently, we want to find  $p_{95}$  such that

$$0.95 = \frac{\Pr[100 < x < p_{95}]}{P[X > 100]} = \frac{F(p_{95}) - F(100)}{1 - F(100)} \text{ where } F(x) \text{ is the distribution function of } X.$$

$$\text{Now } F(x) = 1 - e^{-x/300}.$$

$$\text{Therefore, } 0.95 = \frac{1 - e^{-p_{95}/300} - (1 - e^{-100/300})}{1 - (1 - e^{-100/300})} = \frac{e^{-1/3} - e^{-p_{95}/300}}{e^{-1/3}} = 1 - e^{1/3} e^{-p_{95}/300}$$

$$e^{-p_{95}/300} = 0.05 e^{-1/3}$$

$$p_{95} = -300 \ln(0.05 e^{-1/3}) = 999$$