

74. Solution: E

First note $R = 10/T$. Then

$$F_R(r) = P[R \leq r] = P\left[\frac{10}{T} \leq r\right] = P\left[T \geq \frac{10}{r}\right] = 1 - F_T\left(\frac{10}{r}\right). \text{ Differentiating with respect to}$$

$$r \quad f_R(r) = F'_R(r) = \frac{d}{dr} \left(1 - F_T\left(\frac{10}{r}\right)\right) = -\left(\frac{d}{dt} F_T(t)\right) \left(\frac{-10}{r^2}\right)$$

$$\frac{d}{dt} F_T(t) = f_T(t) = \frac{1}{4} \text{ since } T \text{ is uniformly distributed on } [8, 12].$$

$$\text{Therefore } f_R(r) = \frac{-1}{4} \left(\frac{-10}{r^2}\right) = \frac{5}{2r^2}.$$