

77. Solution: D

$$\text{Prob.} = 1 - \int_1^2 \int_1^2 \frac{1}{8}(x+y) dx dy = 0.625$$

Note

$$\Pr[(X \leq 1) \cup (Y \leq 1)] = \Pr\left\{[(X > 1) \cap (Y > 1)]^c\right\} \quad (\text{De Morgan's Law})$$

$$\begin{aligned} &= 1 - \Pr[(X > 1) \cap (Y > 1)] &&= 1 - \int_1^2 \int_1^2 \frac{1}{8}(x+y) dx dy &&= 1 - \frac{1}{8} \int_1^2 \frac{1}{2}(x+y)^2 \Big|_1^2 dy \\ &= 1 - \frac{1}{16} \int_1^2 [(y+2)^2 - (y+1)^2] dy &&= 1 - \frac{1}{48} [(y+2)^3 - (y+1)^3] \Big|_1^2 &&= 1 - \frac{1}{48} (64 - 27 - 27 + 8) \\ &= 1 - \frac{18}{48} = \frac{30}{48} = 0.625 \end{aligned}$$