

91. Solution: D

We want to find $P[X + Y > 1]$. To this end, note that $P[X + Y > 1]$

$$\begin{aligned} &= \int_0^1 \int_{1-x}^2 \left[\frac{2x+2-y}{4} \right] dy dx = \int_0^1 \left[\frac{1}{2}xy + \frac{1}{2}y - \frac{1}{8}y^2 \right]_{1-x}^2 dx \\ &= \int_0^1 \left[x+1 - \frac{1}{2} - \frac{1}{2}x(1-x) - \frac{1}{2}(1-x) + \frac{1}{8}(1-x)^2 \right] dx = \int_0^1 \left[x + \frac{1}{2}x^2 + \frac{1}{8} - \frac{1}{4}x + \frac{1}{8}x^2 \right] dx \\ &= \int_0^1 \left[\frac{5}{8}x^2 + \frac{3}{4}x + \frac{1}{8} \right] dx = \left[\frac{5}{24}x^3 + \frac{3}{8}x^2 + \frac{1}{8}x \right]_0^1 = \frac{5}{24} + \frac{3}{8} + \frac{1}{8} = \frac{17}{24} \end{aligned}$$