

97. Solution: C

We are given $f(t_1, t_2) = 2/L^2, 0 \leq t_1 \leq t_2 \leq L$.

$$\begin{aligned} \text{Therefore, } E[T_1^2 + T_2^2] &= \int_0^L \int_0^{t_2} (t_1^2 + t_2^2) \frac{2}{L^2} dt_1 dt_2 = \\ &= \frac{2}{L^2} \left\{ \int_0^L \left[\frac{t_1^3}{3} + t_2^2 t_1 \right]_0^{t_2} dt_2 \right\} = \frac{2}{L^2} \left\{ \int_0^L \left(\frac{t_2^3}{3} + t_2^3 \right) dt_2 \right\} \\ &= \frac{2}{L^2} \int_0^L \frac{4}{3} t_2^3 dt_2 = \frac{2}{L^2} \left[\frac{t_2^4}{3} \right]_0^L = \frac{2}{3} L^2 \end{aligned}$$

