

122. Solution: D

The marginal distribution of Y is given by $f_2(y) = \int_0^y 6 e^{-x} e^{-2y} dx = 6 e^{-2y} \int_0^y e^{-x} dx$
 $= -6 e^{-2y} e^{-y} + 6e^{-2y} = 6 e^{-2y} - 6 e^{-3y}, 0 < y < \infty$

Therefore, $E(Y) = \int_0^{\infty} y f_2(y) dy = \int_0^{\infty} (6ye^{-2y} - 6ye^{-3y}) dy = 6 \int_0^{\infty} ye^{-2y} dy - 6 \int_0^{\infty} ye^{-3y} dy =$
 $\frac{6}{2} \int_0^{\infty} 2 ye^{-2y} dy - \frac{6}{3} \int_0^{\infty} 3 ye^{-3y} dy$

But $\int_0^{\infty} 2 ye^{-2y} dy$ and $\int_0^{\infty} 3 ye^{-3y} dy$ are equivalent to the means of exponential random

variables with parameters $1/2$ and $1/3$, respectively. In other words, $\int_0^{\infty} 2 ye^{-2y} dy = 1/2$

and $\int_0^{\infty} 3 ye^{-3y} dy = 1/3$. We conclude that $E(Y) = (6/2) (1/2) - (6/3) (1/3) = 3/2 - 2/3 =$

$9/6 - 4/6 = 5/6 = 0.83$.